

Day 2 on 10-2VII. Properties of logs.

EX 8. $\log_6 \boxed{6^8} = y$ $6^y = 6^8$ $y = 8$

EX 9. $3^{\log_3(4x-1)} = y$ $\log_3 y = \log_3(4x-1)$
 $y = 4x-1$

VIII. Solving log equations.

EX 10. $\log_8 n = \frac{4}{3}$ $8^{(\frac{4}{3})} = \boxed{n = 16}$

EX 11. $\log_5(p^2-2) = \log_5 p$
 $p^2 - 2 = p$
 $p^2 - p - 2 = 0$
 $(p-2)(p+1) = 0$
 $p-2=0$ $p+1=0$
 $\boxed{p=2}$ ~~$\boxed{p=-1}$~~

Can't take the log of a(-) #!

EX 12. $\log_4 x^2 = \log_4(4x-3)$.

$$\begin{aligned} x^2 &= 4x-3 \\ x^2 - 4x + 3 &= 0 \\ (x-3)(x-1) &= 0 \end{aligned}$$

$x = 3, 1$ * Both Check!

IX. Solving inequalities.

If $b > 1$, $x > 0$, and $\log_b x > y$, then $x > b^y$.

If $b > 1$, $x > 0$, and $\log_b x < y$, then $0 < x < b^y$.

EX 13. $\log_5 x < 2$.

$x < 5^2$
 $0 < x < 25$

EX 14. $\log_6 x > 3$.

$$\begin{aligned} x &> 6^3 \\ x &> 216 \end{aligned}$$

EX 15. $\log_{10}(3x-4) < \log_{10}(x+6)$.

$$\begin{aligned} 3x-4 &< x+6 \\ 2x-4 &< 6 \\ 2x &< 10 \\ 4 &< x < 5 \end{aligned}$$

EX 16. $\log_7(2x+8) > \log_7(x+5)$.

$$\begin{aligned} 2x+8 &> x+5 \\ x+8 &> 5 \\ x &> -3 \end{aligned}$$

Check

$$\begin{aligned} 3x-4 &> 0 \\ 3x &> 4 \\ x &> \frac{4}{3} \end{aligned}$$

$$\begin{aligned} x+6 &> 0 \\ x &> -6 \end{aligned}$$

Check

$$\begin{aligned} 2x+8 &> 0 \\ 2x &> -8 \\ x &> -4 \end{aligned}$$

$$\begin{aligned} x+5 &> 0 \\ x &> -5 \end{aligned}$$

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