

Warm-Up

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

1. What is the quadratic formula? _____

2. When do we use the quadratic formula? _____

3. When solving a quadratic, the _____ must be in _____, which means it is equal to _____

4. Solve $x^2 + 4x = 5$.

$$x^2 + 4x - 5 = 0$$

$$a = 1, b = 4, c = -5$$

$$x = \frac{-4 \pm \sqrt{16 - 4(1)(-5)}}{2(1)} = \frac{-4 \pm \sqrt{36}}{2} = \frac{-4 \pm 6}{2}$$

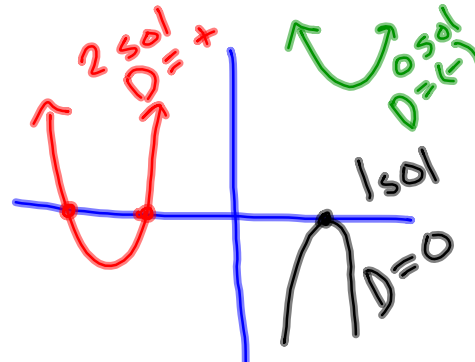
$$\frac{-4 + 6}{2} = \frac{2}{2} = 1$$

$$\frac{-4 - 6}{2} = \frac{-10}{2} = -5$$

Algebra 9-6 Analyzing Solutions to Quadratic Equations

The **discriminant** is used to determine the # of solutions.

Discriminant = $b^2 - 4ac$
 Positive 2 solutions
 Negative 0 solutions
 Zero 1 solution



Examples

3. How many real solutions does the equation $25x^2 - 10x + 1 = 0$ have? 1 solution

$$b^2 - 4ac = 100 - 4(25)(1) \quad a=25, b=-10, c=1$$

$$= 100 - 100 = 0$$

4. How many real solutions does the equation $x^2 + 4 = -6x$ have? 2 solutions

$$b^2 - 4ac = 36 - 4(1)(4) \quad x^2 + 6x + 4 = 0$$

$$= 36 - 16 = 20 \quad a=1, b=6, c=4$$

5. How many real solutions does the equation $3x^2 + 5x + 7 = 0$ have? No Solutions

$$b^2 - 4ac = 25 - 4(3)(7) \quad a=3, b=5, c=7$$

$$= 25 - 84 = -59$$

6. How many real solutions does the equation $x^2 + 38 = 0$ have? No Sol., \emptyset , 0 sol.

$$a=1, b=0, c=38$$

$$b^2 - 4ac = 0 - 4(1)(38)$$

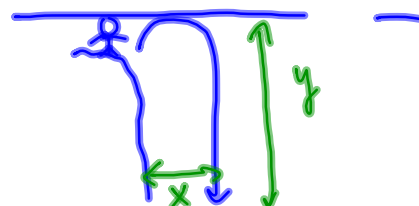
$$= 0 - 152$$

$$= -152$$

Back to the diver from yesterday...

1. The formula $y = -x^2 + 2x + 27$ represents a diver diving, where y is the meters above water and x is the meters away from the cliff.

$y =$ meters above H₂O
 $x =$ meters away from cliff



Will the diver reach a height of...

1. 27.5 meters? yes Why or why not? He starts at 27 m
 when $x=0$, $-(0)^2 + 2(0) + 27 = 27$

2. 28 meters? yes Why or why not? There's a solution
 $28 = -x^2 + 2x + 27$
 $0 = -x^2 + 2x - 1$
 $b^2 - 4ac = 4 - 4(-1)(-1) = 4 - 4 = 0$

3. 29 meters? NO Why or why not? Nope since 28 is the highest point

$$29 = -x^2 + 2x + 27$$

$$0 = -x^2 + 2x - 2$$

$$a = -1, b = 2, c = -2$$

$$b^2 - 4ac = 4 - 4(-1)(-2)$$

$$= 4 - 8$$

$$= -4$$

Assignment: 9.6 #'s 7-16