

3.4 (#2) Name _____
 skip 2, 7, 9, 12, 14

Key

1) A particle travels along the x-axis so that at any time $t \geq 0$, its position is given by $x(t) = t^3 - 9t^2 + 24t + 2$. For what value(s) of t is the velocity equal to zero?

- A) $t = 4$, only
- B) $t = 2$, only
- C) $t = 0$ and $t = 3$
- D) $t = 3$, only
- E) $t = 2$ and $t = 4$**

$$v(t) = x'(t) = 3t^2 - 18t + 24$$

$$= 3(t^2 - 6t + 8)$$

$$= 3(t-2)(t-4)$$

$t = 2 \quad t = 4$

The table below shows the position of a particle, s , at various times, t , as it moves along a straight line.

t (sec)	1.0	1.4	1.8	2.2	2.6
s (ft)	6.0	7.0	10.0	15.0	21.0

What is an estimated value of the velocity of the particle at time $t = 2$?

- A) 15 ft/sec
- B) 12.5 ft/sec**
- C) 20 ft/sec
- D) 10 ft/sec
- E) 5 ft/sec

$$\frac{15 - 10}{2.2 - 1.8} = \frac{5}{.4} = \frac{5}{\frac{2}{5}} = 5 \cdot \frac{5}{2} = \frac{25}{2} = 12.5$$

2) A particle moves on the x-axis so that its position is given by $x(t) = t^4 - 6t^2 + 8$ for $t \geq 0$. For what times t is the velocity of the particle increasing?

- A) $t > 0$
- B) $0 < t < \sqrt{3}$
- C) $t > \sqrt{3}$
- D) $0 < t < 1$
- E) $1 < t < \sqrt{3}$**

$$v(t) = 4t^3 - 12t$$

$$a(t) = 12t^2 - 12$$

$$= 12(t^2 - 1)$$

$$= 12(t+1)(t-1)$$

$t = -1, 1$



6) If the position of a particle moving on the x-axis at any time t is given by $x(t) = 2t^3 - 3t^2$, what is the average acceleration of the particle for $0 \leq t \leq 3$?

- A) 15
- B) 18
- C) 8
- D) 9
- E) 12**

$$v(t) = 6t^2 - 6t$$

$$\frac{v(3) - v(0)}{3 - 0} = \frac{36 - 0}{3} = 12$$

3) The position of a particle moving on a horizontal axis for time t , where $t \geq 0$, is $S(t) = 3 \sin \frac{1}{2}t + 1$. What is the average velocity of the particle for $0 \leq t \leq \frac{3\pi}{2}$?

- A) $\frac{\pi}{\sqrt{2}}$
- B) $\frac{\sqrt{2}}{2}$**
- C) $\frac{3\sqrt{2}}{2}$
- D) $\frac{\pi}{\sqrt{2}}$
- E) $-\frac{\pi}{\sqrt{2}}$

$$\frac{S(\frac{3\pi}{2}) - S(0)}{\frac{3\pi}{2} - 0} = \frac{3\sqrt{2} + 1 - 1}{\frac{3\pi}{2}}$$

$$= \frac{3\sqrt{2}}{2} \cdot \frac{2}{3\pi} = \frac{\sqrt{2}}{\pi}$$

$$v(3) = 6 \cdot 9 - 6 \cdot 3 = 54 - 18 = 36$$

7) A particle moves along the x-axis so that at any time $t \geq 0$, its position is given by $x(t) = 2t + \sin(\pi t)$. What is the acceleration of the particle at time $t = \frac{3}{2}$?

- A) $-\pi^2$
- B) 2
- C) π
- D) π^2**
- E) 0

$$v(t) = 2 + \pi \cos(\pi t)$$

$$a(t) = -\pi^2 \sin(\pi t)$$

$$a(\frac{3}{2}) = -\pi^2 \cdot \sin \frac{3\pi}{2} = -\pi^2 \cdot -1 = \pi^2$$

4) What is the maximum acceleration of a particle on the interval $0 \leq t \leq 3$ if its position is given by $s(t) = t^4 - 4t^3$?

- A) 36**
- B) -16
- C) 0
- D) -12
- E) 24

$$v(t) = 4t^3 - 12t^2$$

$$a(t) = 12t^2 - 24t$$

$$a'(t) = 24t - 24 = 24(t-1) = 0$$

$t = 1$ (max)

$$a(0) = 0$$

$$a(3) = 12(3)^2 - 24(3) = 36 \cdot 3 - 72 = 108 - 72 = 36$$

8) A particle moves along the x-axis so that its position at any time t is given by $x(t) = t^3 - 6t^2 + 9t + 12$. During what times is the speed of the particle increasing?

- A) $t < 1$ or $2 < t < 3$
- B) $1 < t < 2$ or $t > 3$**
- C) $t < 2$ or $t > 3$
- D) $1 < t < 3$
- E) $t < 1$ or $t > 3$

Speeding up \rightarrow look at signs of vel + acc

$$v(t) = 3t^2 - 12t + 9$$

$$0 = 3(t^2 - 4t + 3)$$

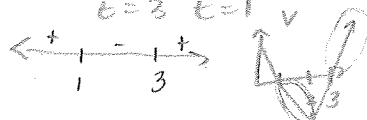
$$0 = 3(t-3)(t-1)$$

$$t = 3 \quad t = 1$$

$$a(t) = 6t - 12$$

$$0 = 6t - 12$$

$$t = 2$$



When v is (-) + decreasing \rightarrow and when v is (+) + increasing

9) A particle moves along a coordinate line so that its position is given by $S(t) = 2 \sin \frac{1}{2}t + \frac{1}{2} \cos 2t$ for $0 \leq t \leq 2\pi$. What is the acceleration of the particle at $t = \pi$?

- A) $-\frac{3}{2}$
- B) $-\frac{1}{2}$**
- C) 1
- D) $-\frac{5}{2}$
- E) $\frac{5}{2}$

Skip trig

Skip

12) A particle moves along a horizontal axis so that its position is defined by $S(t) = 4 \cos \frac{\pi}{2}t$ for $0 \leq t \leq 5$. What is the velocity of the particle at the time its acceleration is first equal to zero?

- A) 2π
- B) -2π
- C) -4π
- D) 4π
- E) $-\pi^2$

Skip Trig

13) A particle moves along a horizontal coordinate line so that its position at time t , $0 \leq t \leq 4$ is given by $S(t) = t^3 - \frac{16}{3}t^2 + 8t + 1$. For what times t is the velocity of the particle decreasing?

- A) $\frac{2}{3} < t < 2$**
- B) $t > \frac{2}{3}$
- C) $0 < t < 2$
- D) $0 < t < 4$
- E) $2 < t < 4$

$$v(t) = 4t^2 - 16t + 8$$

$$a(t) = 8t - 16$$

$$0 = 8t - 16$$

$$t = 2$$



10) A particle moves along the x-axis in such a way that its position at any time t is given by $x(t) = t^3 - 8t^2 + 18t + 2$ for $t > 0$. At what time is acceleration of the particle equal to 36?

- A) 3
- B) 4**
- C) 12
- D) 6
- E) 2

$$v(t) = 4t^2 - 16t + 18$$

$$a(t) = 8t - 16$$

$$36 = 8t - 16$$

$$0 = 8t - 52$$

$$0 = 2t(t - 4)$$

$$t = 0, t = 4$$

\uparrow

Add 2 table

14) The table below shows velocity of a particle at various times t of a particle that moves along a horizontal line.

t (sec)	0.5	1.0	1.5	2.0	2.5
v (m/sec)	8.3	9.2	9.8	10.6	11

What is an approximate value of the acceleration of the particle at time $t = 2$?

- A) 1.2 ft/sec²**
- B) -0.8 ft/sec²
- C) 1.6 ft/sec²
- D) -1.6 ft/sec²
- E) 1.8 ft/sec²

(1.5, 9.8)
(2.5, 11)

$$\frac{\Delta v}{\Delta t} = \frac{11 - 9.8}{2.5 - 1.5} = \frac{1.2}{1} = 1.2$$

11) A particle moves on the x-axis such that its position at any time $t > 0$ is given by $x(t) = t^3 - 9t^2 + 24t$. What is the velocity of the particle when its acceleration is zero?

- A) 105
- B) 24
- C) -3**
- D) 3
- E) 0

$$v(t) = 3t^2 - 18t + 24$$

$$a(t) = 6t - 18$$

$$0 = 6t - 18$$

$$18 = 6t$$

$$t = 3$$

$$v(3) = 3(3)^2 - 18(3) + 24$$

$$= -3$$