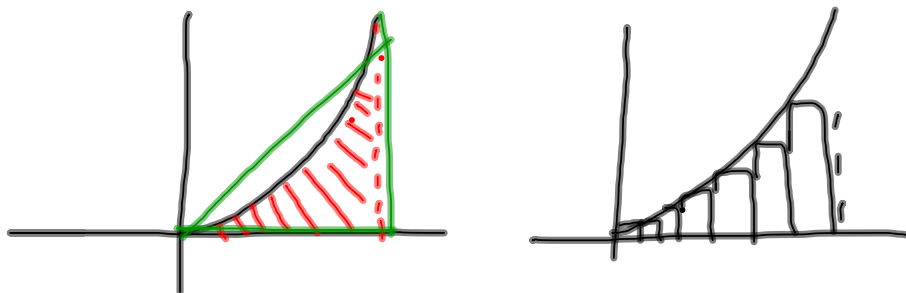


## 5.1 Estimating with Finite Sums

$$\int_a^b f(x) dx \rightarrow \text{Find the area between the curve } f(x) \text{ and the } x\text{-axis between } [a, b]$$

↳ sum



RAM = Rectangle Approximation Method

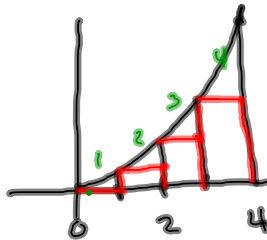
**L**RAM - **Left** Rectangle Approximation Method

**R**RAM - **Right** Rectangle Approximation Method

**M**RAM - **Midpoint** Rectangle Approximation Method

Ex 1) Estimate the area under  $y = x^2$   $[0, 4]$  using 4 rectangles.

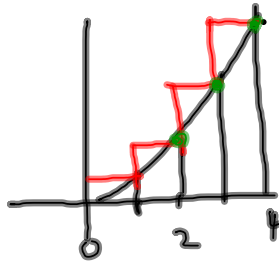
**LRAM**



$A = bh$

- #1 =
- #2 =
- #3 =
- #4 =

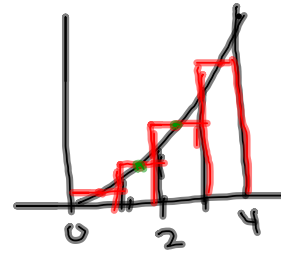
**RRAM**



$A = bh$

- #1 =
- #2 =
- #3 =
- #4 =

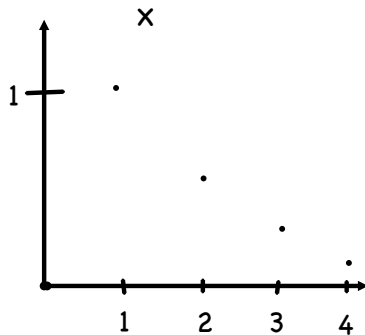
**MRAM**



$A = bh$

- #1 =
- #2 =
- #3 =
- #4 =

Ex 2)  $y = \frac{1}{x}$  Estimate the area in the interval  $[2, 4]$  using 4 rectangles.



base =  $\frac{b - a}{\text{\# of rectangles}}$

**LRAM**

$A = bh$

- #1 =
- #2 =
- #3 =
- #4 =

**RRAM**

$A = bh$

- #1 =
- #2 =
- #3 =
- #4 =

**MRAM**

$A = bh$

- #1 =
- #2 =
- #3 =
- #4 =