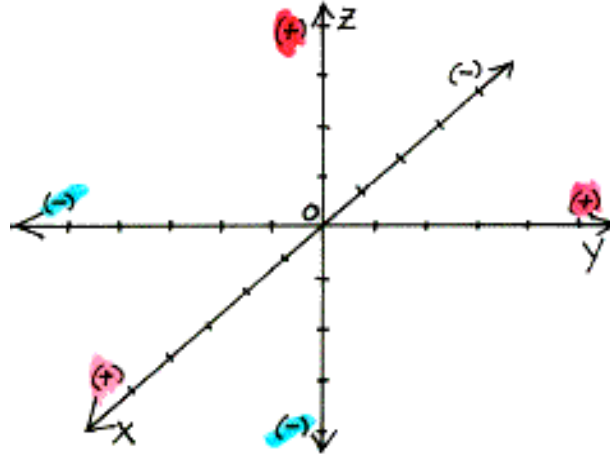


13-5 Coordinates in Space

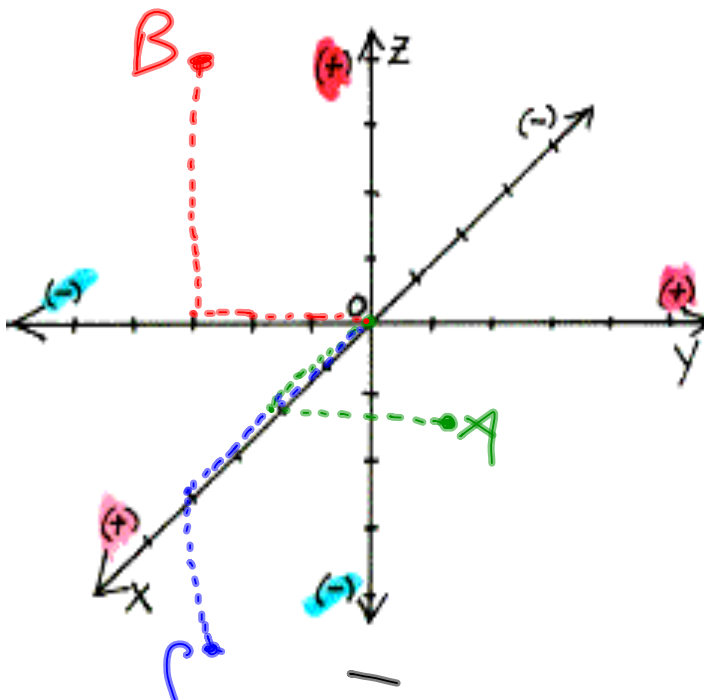
Ordered Triple:

* How a point in space is represented.

* (x, y, z)



1. Plot the following points:



A $(\overset{x}{2}, \overset{y}{3}, \overset{z}{0})$

B $(\overset{x}{0}, \overset{y}{-3}, \overset{z}{4})$

C $(\overset{x}{4}, \overset{y}{0}, \overset{z}{-2})$

Distance:

- * The distance between points in space can be found by using a special case of the distance formula.

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

2. Determine the distance between F (4, -2, 0) and G (-2, 3, -1).

$$\begin{aligned} & \sqrt{(-2-4)^2 + (3+2)^2 + (-1-0)^2} \\ & \sqrt{(-6)^2 + (5)^2 + (-1)^2} \\ & \sqrt{36 + 25 + 1} \\ & \sqrt{62} \end{aligned}$$

Midpoint:

- * The midpoint in space between two points can be found by using a special midpoint formula.

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}, \frac{z_1 + z_2}{2} \right)$$

3. Determine the midpoint M of segment FG if F (4, -2, 0) and G (-2, 3, -1)

$$\begin{aligned} \text{Midpt. of FG} &= \left(\frac{4+(-2)}{2}, \frac{-2+3}{2}, \frac{0+(-1)}{2} \right) \\ &= \left(1, \frac{1}{2}, -\frac{1}{2} \right) \end{aligned}$$

Translations (slides):

* Can be performed in space

$$* (x, y, z) \text{-----} (x + a, y + b, z + c)$$

4. Translate the following points using the following translations.

B (0, -5, 8): $(x, y, z) \text{----} (x - 4, y + 3, z - 5)$

$$(0 - 4, -5 + 3, 8 - 5)$$

$$(-4, -2, 3)$$

Dilation's (size changes) can also be performed in space.

$$(x, y, z) \text{-----} k(x, y, z) = (kx, ky, kz)$$

5. Perform the indicated dilations for the ordered triple.

a. $(3, 0, -4)$ with $k = 2$

$$(2 \cdot 3, 2 \cdot 0, 2 \cdot -4)$$

$$(6, 0, -8)$$