

Pythagorean Theorem:

* Given a right triangle, *then*

$$a^2 + b^2 = c^2$$

$$* \text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

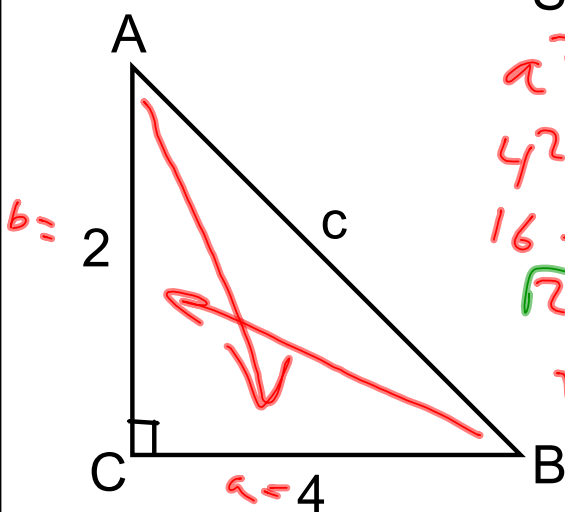
Converse of Pythagorean Theorem:

If $a^2 + b^2 = c^2$, then the triangle is a right triangle.

Pythagorean Triple:

* Three **whole** numbers that satisfy the equation $a^2 + b^2 = c^2$ where c is the greatest number.

* Examples: 3, 4, 5 6, 8, 10

Example 1:

Solve for c.

$$a^2 + b^2 = c^2$$

$$4^2 + 2^2 = c^2$$

$$16 + 4 = c^2$$

$$\sqrt{20} = \sqrt{c^2}$$

$$\sqrt{20} = c$$

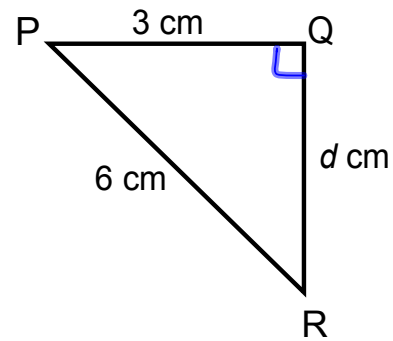
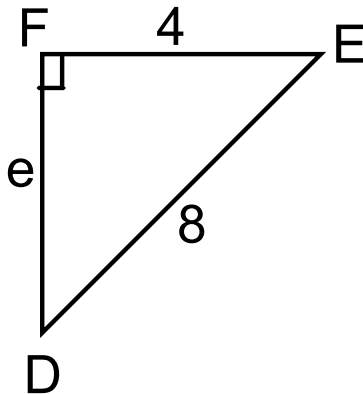
$$\sqrt{4 \cdot 5} = c$$

$$2\sqrt{5} = c$$

7-2 Pythagorean Theorem

Example 2: Find d .

$$\begin{aligned}
 d^2 + 3^2 &= 6^2 \\
 d^2 + 9 &= 36 \\
 \underline{-9 \quad -9} & \\
 \sqrt{d^2} &= \sqrt{27} \\
 d &= \sqrt{27} \\
 d &= \sqrt{3 \cdot 9} \\
 d &= 3\sqrt{3} \text{ cm}
 \end{aligned}$$

**Example 3:**Solve for e .

$$\begin{aligned}
 e^2 + 4^2 &= 8^2 \\
 e^2 + 16 &= 64 \\
 \underline{-16 \quad -16} & \\
 \sqrt{e^2} &= \sqrt{48} \\
 e &= \sqrt{48} \\
 e &= \sqrt{16 \cdot 3} \\
 e &= 4\sqrt{3}
 \end{aligned}$$

Example 4:

Determine whether each set of measures are the sides of a right triangle. Then state if they form a Pythagorean Triple.

a. ^a9, ^b12, and ^c15

$$a^2 + b^2 = c^2$$

Yes, right Δ

$$9^2 + 12^2 = 15^2$$

Yes, Pyth. triple

$$81 + 144 = 225$$

$$225 = 225 \checkmark$$

b. ^a21, ^b42, and ^c54

$$21^2 + 42^2 = 54^2$$

NO, not a right Δ .

$$441 + 1764 = 2916$$

$$2205 \neq 2916$$

c. ^a $4\sqrt{3}$, ^b4 and ^c8

$$(4\sqrt{3})^2 + 4^2 = 8^2$$

Yes, right Δ .

$$4^2 \cdot (\sqrt{3})^2$$

no Pyth. triple

$$16 \cdot 3 + 16 = 64$$

$$48 + 16 = 64$$

$$64 = 64 \checkmark$$