

2.4 Complex Conjugates Day 2I. Complex Conjugates-- $a + bi$, $a - bi$ Find the conjugate and multiply.

Ex 1) $(7 - 5i)(7 + 5i)$

$$\begin{aligned} & 49 - 25i^2 \\ & 49 + 25 = \boxed{74} \end{aligned}$$

Ex 2) $(-6 - \sqrt{5}i)(-6 + \sqrt{5}i)$

$$\begin{aligned} & 36 - 5i^2 \\ & 36 + 5 = \boxed{41} \end{aligned}$$

II. Write the quotient in standard form.

Ex 3) $\frac{(2 + 3i)(4 + 2i)}{(4 - 2i)(4 + 2i)} = \frac{8 + 16i + 6i^2}{16 - 4i^2} = \frac{8 + 16i - 6}{16 + 4}$

$$\begin{aligned} & \frac{i^2 + 2 + 16i + i^2}{20 \div 2} = \frac{1 + 8i}{10} = \frac{1}{10} + \frac{8i}{10} = \boxed{\frac{1}{10} + \frac{4}{5}i} \end{aligned}$$

Ex 4) $\frac{6}{i} \cdot \frac{i}{i} = \frac{6i}{i^2} = \boxed{-6i}$ or $\boxed{0 - 6i}$

III. Perform the operation and write in standard form.

$$\text{Ex 5) } \frac{i}{3-2i} + \frac{2i}{3+2i} = \frac{-i(3+2i)}{(3-2i)(3+2i)} + \frac{2i(3-2i)}{(3-2i)(3+2i)} = \frac{3i+2i^2+6i^2-4i^2}{(3-2i)(3+2i)}$$

$$\frac{2+9i}{(3-2i)(3+2i)} = \frac{2+9i}{9-4i^2} = \frac{2+9i}{9+4} = \frac{2+9i}{13}$$
$$= \frac{2}{13} + \frac{9}{13}i$$